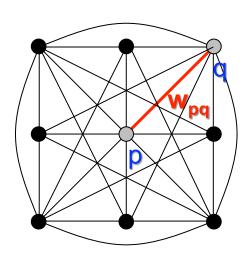
# Image Segmentation continued Graph Based Methods

Some slides: courtesy of O. Capms, Penn State, J.Ponce and D. Fortsyth, Computer Vision Book

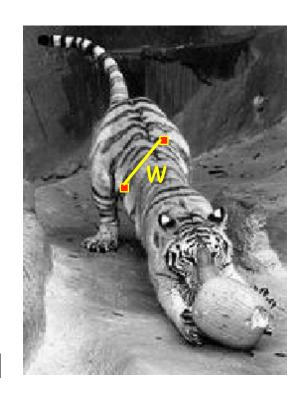
# Previously

- Binary segmentation
- Segmentation by thresholding
- Background subtraction
- Motion segmentation
- K-means clustering
- Grouping and graph based segmentation

# Images as graphs



- Fully-connected graph
  - node (vertex) for every pixel
  - link between every pair of pixels, p,q
  - affinity weight w<sub>pq</sub> for each link (edge)
    - w<sub>pq</sub> measures similarity
      - similarity is *inversely proportional* to difference (in color and position...)



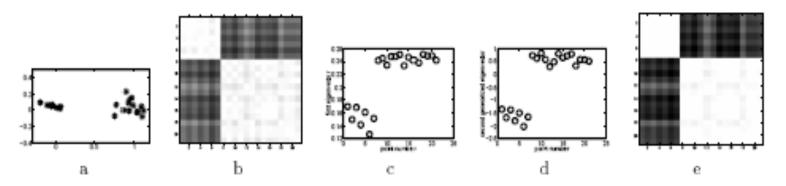
# Segmentation as Graph Partitioning

- (Shi & Malik ''97)
- Idea each pixel in the image is a node in the graph
- Arcs represent similarities between adjacent pixels
- Graph is fully connected
- Goal partition the graph into a sets of vertices (regions), such that the similarity within the region is high – and similarity across the regions is low.
- See textbook (Ponce and Forsythe) for detailed description the algorithm.



# Segmentation

- Toy example
- Bright entries in the affinity matrix high
- Likely to belong together

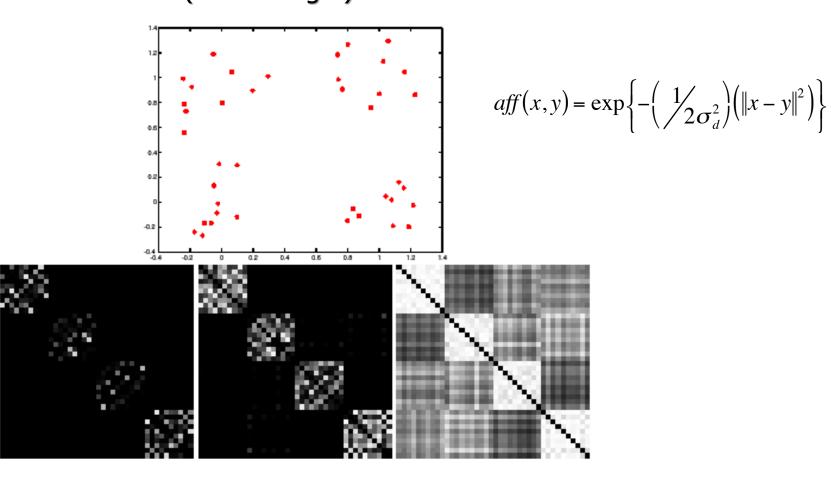


one possible affinity based on distance

$$aff(x,y) = \exp\left\{-\left(\frac{1}{2\sigma_d^2}\right)\left(\|x - y\|^2\right)\right\}$$

# Scale affects affinity

Depending on the scale the blocks are more (middle) Or less obvious (left and right)



$$\sigma_d = \{0.1, 0.2, 1\}$$

# **Measuring Affinity**

Intensity

$$aff(x,y) = \exp\left\{-\left(\frac{1}{2\sigma_i^2}\right)\left(\|I(x) - I(y)\|^2\right)\right\}$$

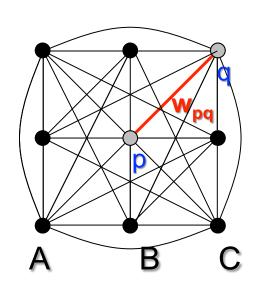
Distance

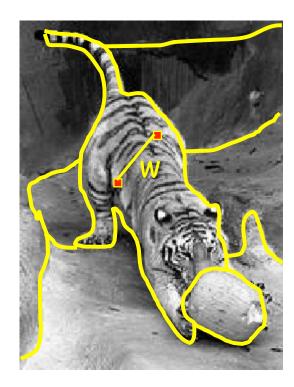
$$aff(x,y) = \exp\left\{-\left(\frac{1}{2\sigma_d^2}\right)\left(\|x - y\|^2\right)\right\}$$

**Texture** 

$$aff(x,y) = \exp\left\{-\left(\frac{1}{2\sigma_t^2}\right)\left(\|c(x) - c(y)\|^2\right)\right\}$$

# Segmentation by Graph Cuts

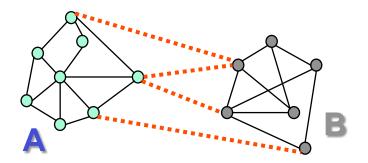




- Break Graph into Segments
  - Want to delete links that cross between segments
  - Easiest to break links that have low similarity (low weight)
    - similar pixels should be in the same segments
    - dissimilar pixels should be in different segments

Source: Steve Seitz

# Cuts in a graph: Min cut



#### Link Cut

set of links whose removal makes a graph disconnected

- cost of a cut: 
$$cut(A,B) = \sum_{p \in A, q \in B} w_{p,q}$$

#### Find minimum cut

- · gives you a segmentation
- fast algorithms exist for doing this

Source: Steve Seitz

#### Minimum cut

Problem with minimum cut:
 Weight of cut proportional to number of edges in the cut; tends to produce small, isolated components.

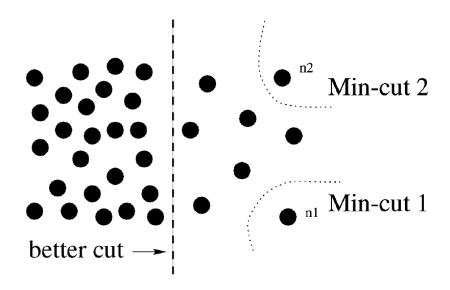
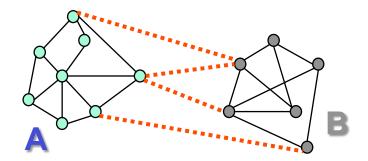


Fig. 1. A case where minimum cut gives a bad partition.

# Cuts in a graph: Normalized cut



#### **Normalized Cut**

fix bias of Min Cut by normalizing for size of segments:

$$Ncut(A, B) = \frac{cut(A, B)}{assoc(A, V)} + \frac{cut(A, B)}{assoc(B, V)}$$

assoc(A,V) = sum of weights of all edges that touch A

- Ncut value small when we get two clusters with many edges with high weights, and few edges of low weight between them
- Approximate solution for minimizing the Ncut value : generalized eigenvalue problem.

Source: Steve Seitz

# Eigenvectors and segments

- Simplest idea: we want a vector giving the association between each element and a cluster
- We want elements within this cluster to, on the whole, have strong affinity with one another
- We could maximize

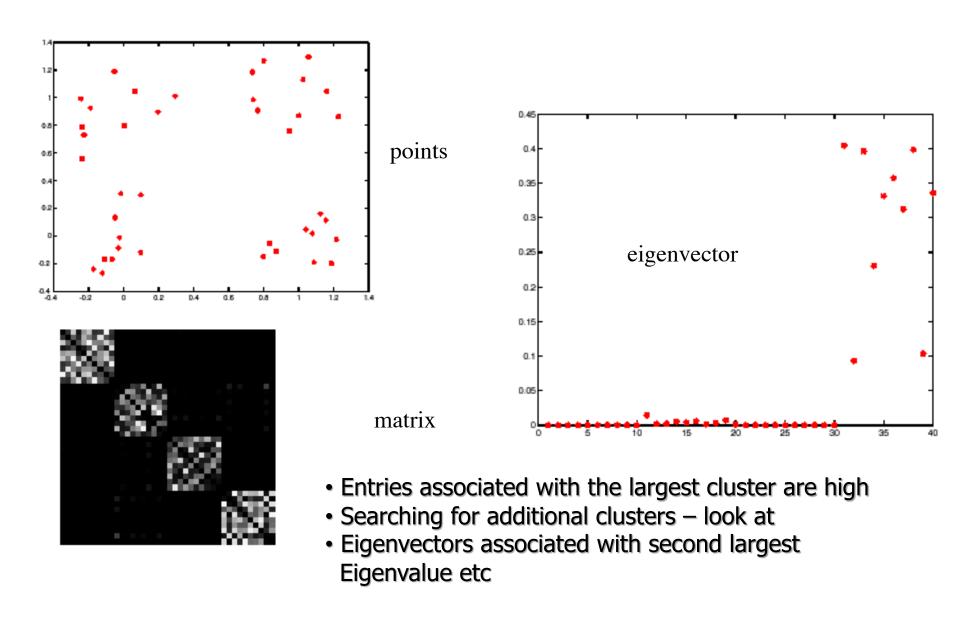
 $a^{T}Aa$ 

But need the constraint

$$a^{T}a = 1$$

 This is an eigenvalue problem - choose the eigenvector of A with largest eigenvalue - single good cluster

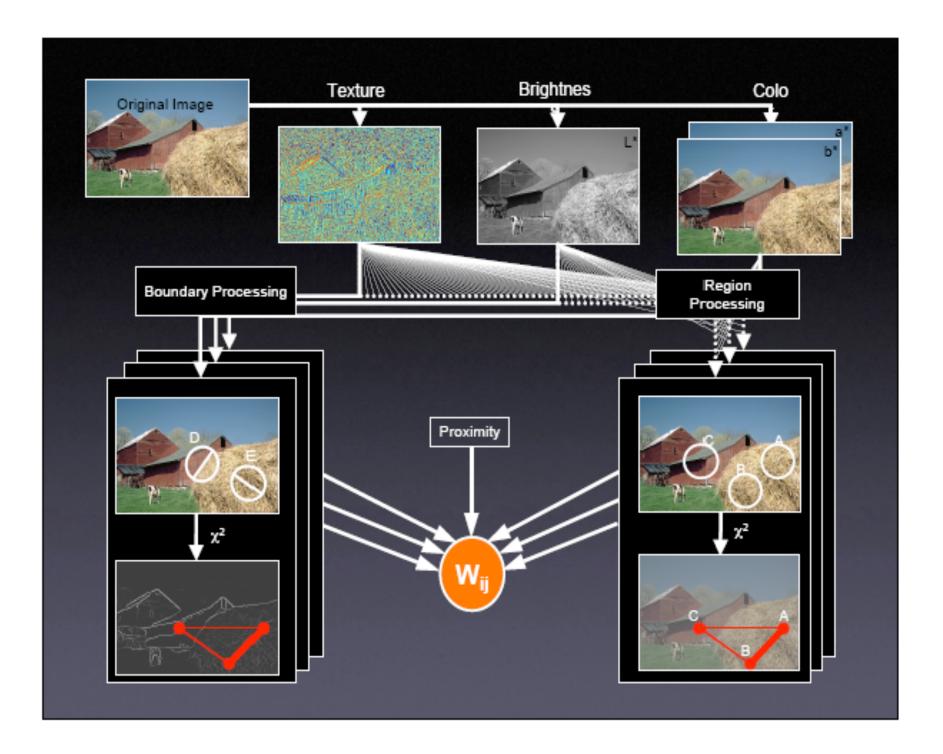
# Example eigenvector



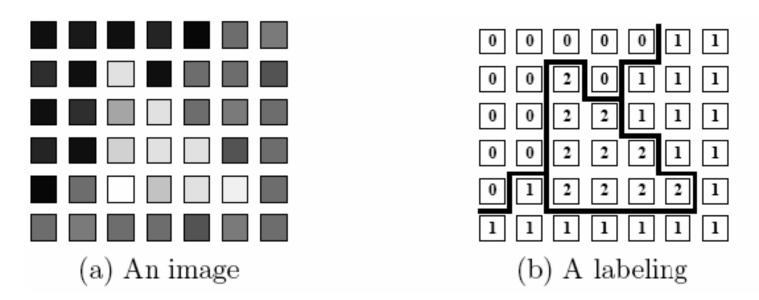
## More than two segments

- Reasoning about other eigenvectors consider that affinity matrix is block diagonal.
- Until there are sufficient clusters pick eigenvector associated with the largest eigenvalue, zero the elements which were clustered, threshold elements with large association weights those will form a new cluster
- Keep going until there is sufficient number of clusters and all elements have been accounted for
- Spectral Clustering Techniques (A. Ng and M. Jordan)
- Problems if the eigenvalues are similar eigenvectors do not reveal the clusters
- Normalized cut graph cut alternative optimization criterion J.
   Shi and J. Malik derivation on the board





# Graph Cuts, MRF's

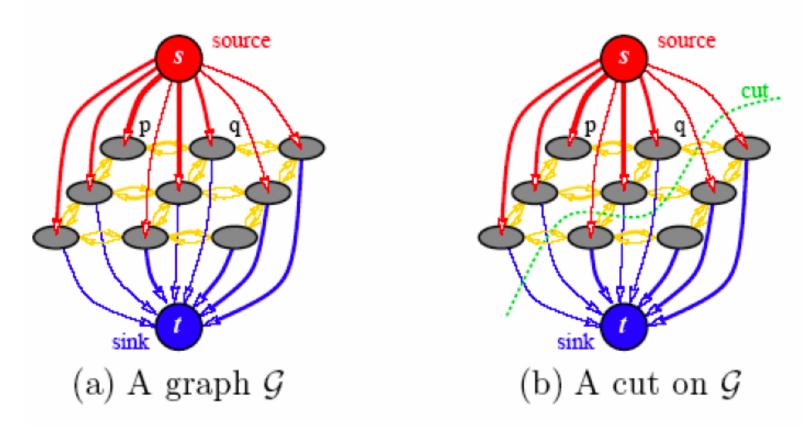


Pixel labeling problem - find such labels that the objective function is minimized labels (stereo, object/no-object, original intensities (denoising)

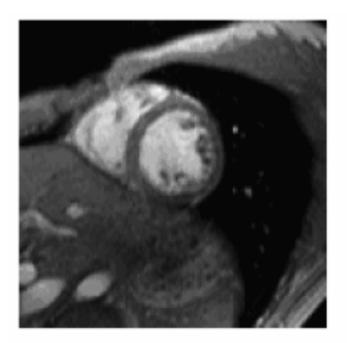
$$E(f) = \sum_{p \in P} D_p(f_p) + \sum_{p,q \in N} V_{p,q}(f_p, f_q)$$

J. Kosecka

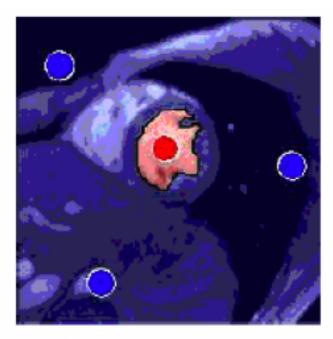
# **Graph Cut**



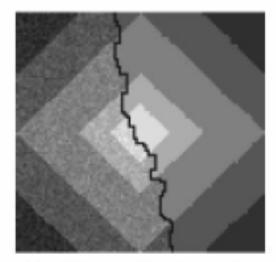
Formulated as minimum cost flow -Network flow problem from Graph Theory Kolmogorov, Boykov (et al) efficient solvers available



Original image



A minimum cut

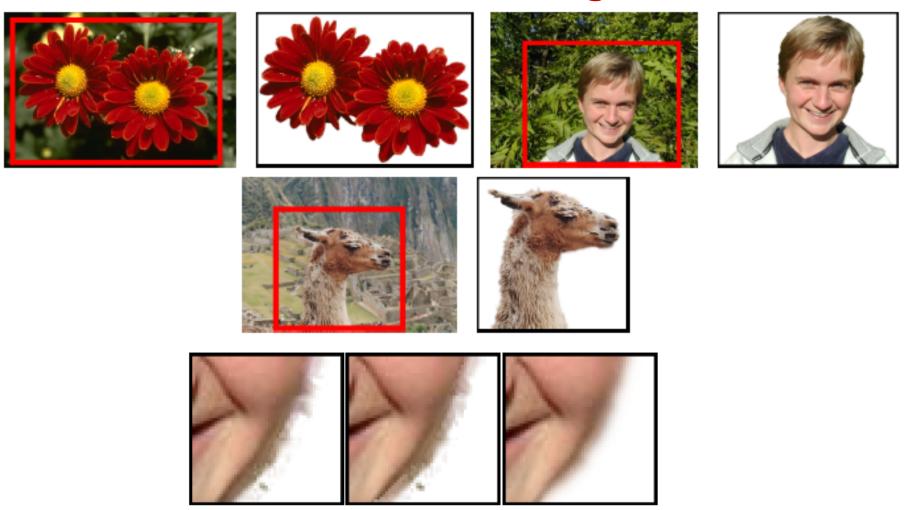




(a) Diamond restoration (b) Original Bell Quad (c) "Restored" Bell Quad



# Interactive Foreground Segmentation



Interaction Foreground Segmentation: Grab Cuts Rother, Kolmogorov, Blake, SIGRAPH 2005

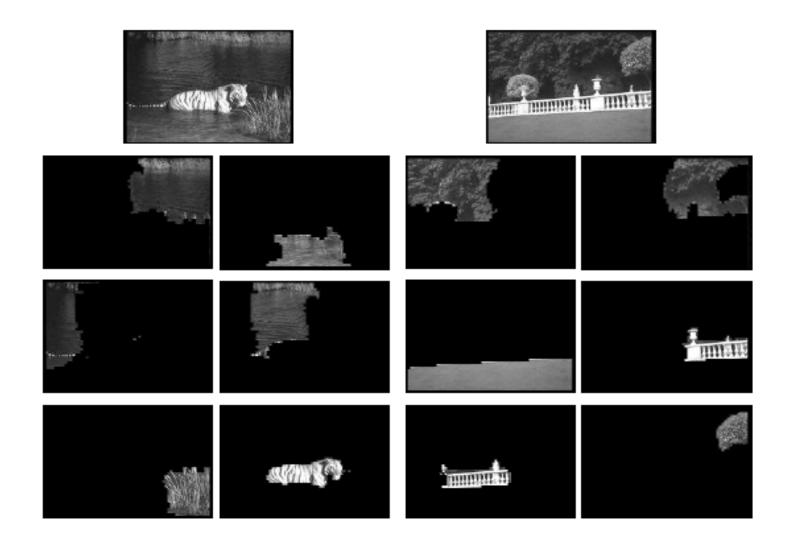


Figure from "Image and video segmentation: the normalised cut framework", by Shi and Malik, copyright IEEE, 1998

# Example results



# Results: Berkeley Segmentation Engine



http://www.cs.berkeley.edu/~fowlkes/BSE/

# Normalized cuts: pros and cons

## Pros:

- Generic framework, flexible to choice of function that computes weights ("affinities") between nodes
- Does not require model of the data distribution

#### Cons:

- Time complexity can be high
  - Dense, highly connected graphs → many affinity computations
  - Solving eigenvalue problem
- Preference for balanced partitions

# **Graph Based Segmentation**

- Given representation of an image as a graph G(V,E)
- Partition the graph into C components, such that all the nodes within a component are similar
- Minimum weight spanning tree algorithm
- 1. Start with pixels as vertices, edge as similarity between neigbours, gradualy build connected components of the graph
- 2. Pick the lowest cost edge, the decision whether to join the two components or keep them apart depends on similarity within the components is smaller then similarity between the components. If the difference between the components is small then join them, else do nothing
- 3. Stopping criterion number of desired segments

Ref. P. Felzenswalb and D. Huttenlocher Efficient Graph Based Image Segmentation

# MWST graph based segmentation

# • Example results









# Segments as primitives for recognition

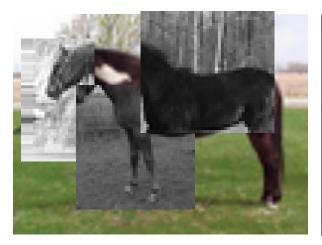
**Multiple segmentations** The ! ! of Islay Life NO VEHICULAR, ACCESS BEYOND THIS POINT No toading I Townson's

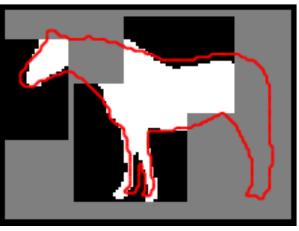
B. Russell et al.,

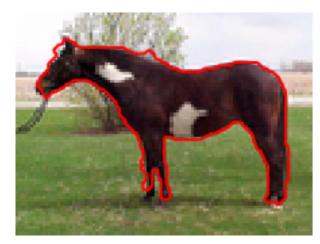
"Using Multiple Segmentations to Dis

"Using Multiple Segmentations to Discover Objects and shadic Extention Lazebnik Image Collections," CVPR 2006

# Top-down segmentation



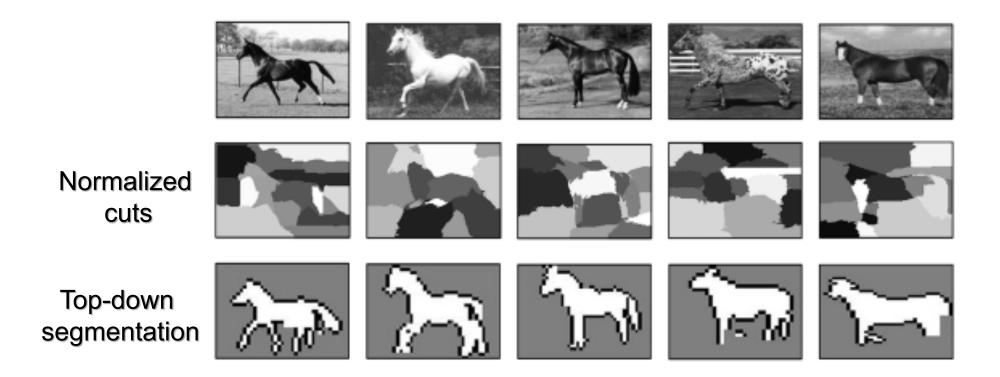




- E. Borenstein and S. Ullman, "Class-specific, top-down segmentation," ECCV 2002
- A. Levin and Y. Weiss, "Learning to Combine Bottom-Up and Top-Down Segmentation," ECCV 2006.

Slide credit: Lana Lazebnik

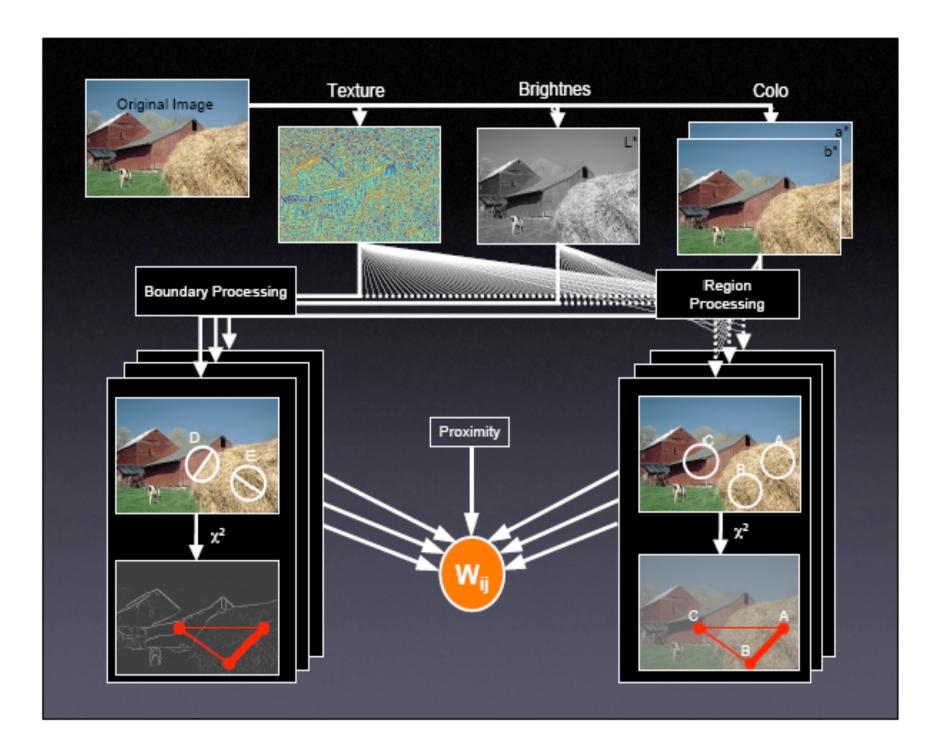
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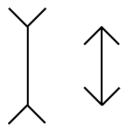
# Technique: Shot Boundary Detection

- Find the shots in a sequence of video
  - shot boundaries usually result in big differences between succeeding frames
- Strategy:
  - compute interframe distances
  - declare a boundary where these are big

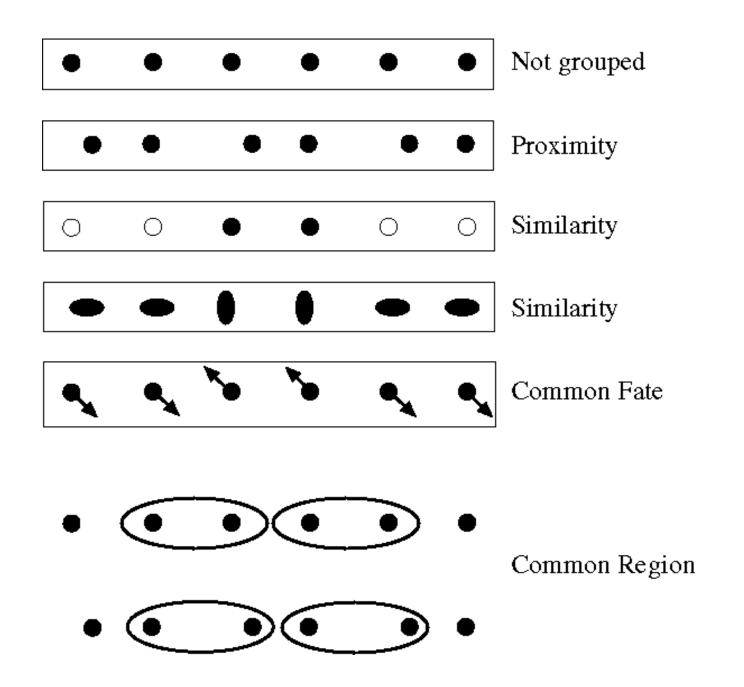
- Possible distances
  - frame differences
  - histogram differences
  - block comparisons
  - edge differences
- Applications:
  - representation for movies, or video sequences
    - find shot boundaries
    - obtain "most representative" frame
  - supports search

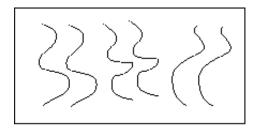
# Grouping in humans

- Figure-ground discrimination
  - grouping can be seen in terms of allocating some elements to a figure, some to ground
  - impoverished theory

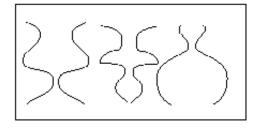


- Gestalt properties
  - elements in a collection of elements can have properties that result from relationships (Muller-Lyer effect)
    - Gestalt-qualitat
  - A series of factors affect whether elements should be grouped together
    - Gestalt factors

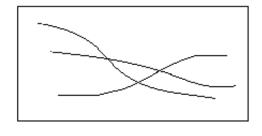




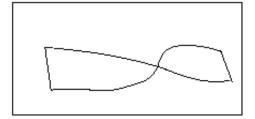
#### Parallelism



Symmetry



Continuity



Closure



